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Data-driven vs model-driven

Data-driven methods for predictive modelling

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October 24, 2023

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Statistical modelling

- Statistics starts with data: something we have measured
- Data is generated by some (unknown) mechanism: input (stimulus) x, output (response) y
- Before analysis this is a black box to us, we only have the data itself
- Two goals of analysis:
 - Prediction of future responses, given known inputs
 - **2 Explanation**, **Understanding** of what is in the "black box" (i.e., make it "white" or at least "some shade of grey").

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Data modelling (also called "model-based")

- assume an empirical-statistical (stochastic) data model for the inside of the black box, e.g., a functional form such as multiple linear, exponential, hierarchical ...
- parameterize the model from the data
- evaluate the model using model diagnostics

Algorithmic modelling (also called "data-driven")

- find an algorithm that produces y given x
- evaluate by predictive accuracy (note: not internal accuracy)

Reference: Breiman, L. (2001). Statistical Modeling: The Two Cultures (with comments and a rejoinder by the author). Statistical Science, 16(3), 199–231.

https://doi.org/10.1214/ss/1009213726

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Explanation vs. prediction

Explanation

- Testing a **causal theory** why are things the way they are?
- Emphasis is on correct model specification and coefficient estimation
- Uses conceptual variables based on theory, which are represented by measureable variables

Prediction

- Predicting new (space, members of population) or future (time) observations.
- Uses measureable variables only, no need for concepts

Reference: Shmueli, G. (2010). To Explain or to Predict? Statistical Science, 25(3),

289-310. https://doi.org/10.1214/10-STS330

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Data-driven vs model-driven methods The expected prediction error (EPE) for a new observation with value x is:

EPE =
$$\mathbb{E}\{Y - \widehat{f(x)}\}^2$$

= $\mathbb{E}\{Y - f(x)\}^2 + \{\mathbb{E}(\widehat{f(x)}) - f(x)\}^2$
 $+ \mathbb{E}\{\widehat{f(x)} - \mathbb{E}(\widehat{f(x)})\}^2$
= $\operatorname{Var}(Y) + \operatorname{Bias}^2 + \operatorname{Var}(\widehat{f(x)})$

Model variance: residual error with perfect model specification (i.e., noise in the relation)

Bias: mis-specification of the statistical model: $\widehat{f(x)} \neq f(x)$

Estimation variance: the result of using a sample to estimate $\widehat{f(x)}$

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Explanation vs. prediction

Bias/variance tradeoff: explanation vs. prediction

Explanation Bias should be minimized

 correct model specification and correct coefficients → correct conclusions about the theory (e.g., causual relation)

Prediction **Total EPE** should be minimized.

- accept some bias if that reduces the estimation variance
- a simpler model (omitting less important predictors) often has better fit to the data

When does an underspecified model better predict than a full model?

Explanation vs.

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- the data are very **noisy** (large σ of the target variable, even with a perfect model);
- the true absolute values of the omitted parameters are small;
- the predictors are highly correlated; and
- the sample size is small or the range of omitted variables is narrow.

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Problems with data modelling

- Mosteller and Tukey(1977): "The whole area of guided regression [an example of, model-based inference] is fraught with intellectual, statistical, computational, and subject matter difficulties."
- It seems we understand nature if we fit a model form, but in fact our conclusions are about the model's mechanism, and not necessarily about nature's mechanism.
- So, if the model is a poor emulation of nature, the conclusions about nature may be wrong ...
- ...and of course the predictions may be wrong we are incorrectly extrapolating.

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Data-driven vs model-driven

The philosophy of data-driven methods

- Also called "statistical learning", "machine learning"
- Build structures to represent the "black box" without using a statistical model
- Model quality is evaluated by predictive accuracy on test sets covering the target population
 - cross-validation methods can use (part of) the original data set if an independent set is not available

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Some data-driven methods

- Covered in this lecture
 - Classification & Regression Trees (CART) 分类与回归树
 - Random Forests (RF) 随机森林
 - Cubist
- Others
 - Artificial Neural Networks (ANN) 人工神经网络
 - Support Vector Machines
 - Gradient Boosting (xgboost
- Relevant R packages: https: //cran.r-project.org/web/views/MachineLearning.html

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- James, G., Witten, D., Hastie, T., & Tibshirani, R. (2021). An introduction to statistical learning: with applications in R (second edition). New York: Springer. https://doi.org/10.1007/978-1-0716-1418-1
- Stanford online course, based on James et al. book: https://www.edx.org/course/statistical-learning?index= product&queryID=d36d87b77d62e1e9ba8218e5f169cf38&position=1
- Kuhn, M., & Johnson, K. (2013). Applied Predictive Modeling (2013 edition). New York: Springer. https://doi.org/10.1007/978-1-4614-6849-3

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- Shmueli, G. (2010). To Explain or to Predict? Statistical Science, 25(3), 289–310. https://doi.org/10.1214/10-STS330
- P Breiman, L. (2001). Statistical Modeling: The Two Cultures (with comments and a rejoinder by the author). Statistical Science, 16(3), 199–231. https://doi.org/10.1214/ss/1009213726
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Classification & Regression Trees (CART)

Decision trees 决策树

- Typical uses in diagnostics (medical, automotive ...)
- Begin with the full set of possible decisions
- Split into two (binary) subsets based on the values of some decision criterion
- Each branch has a more limited set of decisions, or at least has more information to help make a decision
- Continue recursively on both branches until there is enough information to make a decision

Engineering Flowchart



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Classification & (CART)

Regression Trees

Classification & Regression Trees 分类与回归树

- A type of decision tree; decision is "what is the predicted response, given values of predictors"?
- Aim is to predict the **response** (target) variable from one or more **predictor** variables
- If response is categorical (class, factor) we build a classification tree
- If response is continuous we build a regression tree
- *Predictors* can be any combination of categorical or continuous

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Advantages of CART

- A simple model, no statistical assumptions other than between/within class variance to decide on splits
 - For example, no assumptions of the distribution of residuals
 - So can deal with non-linear and threshold relations
- No need to transform predictors or response variable
- Predictive power is quantified by cross-validation; this also controls complexity to avoid over-fitting

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Disadvantages of CART

- No model coefficients to interpret
 - although we can see variable importance overall and influence on each prediction
- Predictive power over a population depends on a sample that is representative of that population
- Quite sensitive to the sample, even when pruned
- Pruning to a complexity parameter depends on 10-fold cross-validation, which is sensitive to the choice of observations in each fold
- Typically makes only a small number of different predictions ("boxes"), so maps made with it show discontinuities ("jumps")

Data-driven methods for predictive modelling R packages

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Data-driven vs. model-driven rpart: "Recursive partitioning for classification, regression and survival trees. An implementation of most of the functionality of the 1984 book by Breiman, Friedman, Olshen and Stone"¹

 good introduction: vignette("longintro", package="rpart")

• rpart.plot: Plot rpart models

¹Breiman, L., Friedman, J. H., Olshen, R. A., & Stone, C. J. (1984). Classification and regression trees. Wadsworth

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Tree terminology

- splitting variable variable to examine, to decide which branch of the tree to follow
- root node 根部节点 variable used for first split; overall mean and total number of observations
- **interior node** 非叶子节点 splitting variable, value on which to split, mean and number to be split
- leaf 叶子点 predicted value, number of observations contributing to it
- cutpoint of the splitting variable: value used to decide which branch to follow
- growing the tree
- pruning the tree

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Example regression tree

- Meuse River soil heavy metals dataset
- Response variable: log₁₀Zn concentration in topsoil
- **Predictor** variables
 - 1 distance to Meuse river (continuous)
 - elevation above sea level (continuous)
 - 3 flood frequency class (categorical, 3 classes)

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Meuse River study area. Sample points, with Zn concentrations as proportional-size circles, shown in Google Earth

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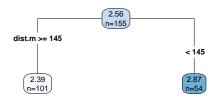
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Example regression tree – first split



Splitting variable: distance to river

Is the point closer or further than 145 m from the river? 101 points *yes*, 54 points *no*.

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Explanation of first split

- root: average log₁₀Zn of whole dataset 2.56 log(mg kg⁻¹) fine soil; based on all 155 observations
- splitting variable at root: distance to river
- cutpoint at root: 145 m
- leaves
 - distance < 145 m: 54 observations, their mean is 2.87 log(mg kg⁻¹)
 - distance ≥ 145 m: 101 observations, their mean is 2.39 log(mg kg⁻¹)
 - full dataset has been split into two more homogeneous subsets

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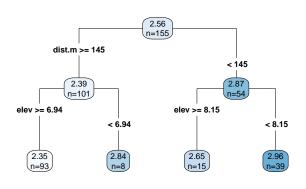
Predictor

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Example regression tree – second split



For both branches, what is the elevation of the point?

Note: this is a coincidence in this case, different splitting variables can be used on different branches.

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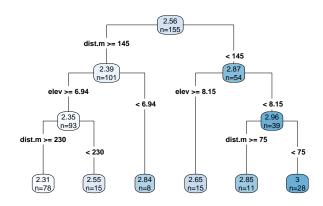
Explanation of second split

- interior nodes were leaves after the first split, now 'roots' of subtrees
 - *left*: distance \geq 145 m: 101 observations, their mean is 2.39 $log(mg \ kg^{-1})$ note smaller mean on left
 - right: distance < 145 m: 54 observations, their mean is 2.87 $log(mg kg^{-1})$
- splitting variable at interior node for < 145 m: elevation
- cutpoint at interior node for < 145 m: 8.15 m.a.s.l.
- splitting variable at interior node for ≥ 145 m: elevation
- cutpoint at interior node for ≥ 145 m: 6.95 m.a.s.l.
- leaves 93, 8, 15, 39 observations; means 2.35, 2.84, 2.65, 2.96 log(mg kg⁻¹)
- These leaves are now more homogeneous than the interior nodes.

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Regression trees

Example regression tree - third split



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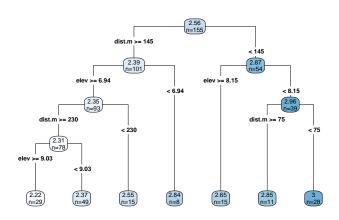
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Example regression tree – fourth split



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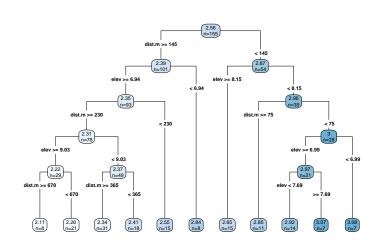
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Example regression tree – fifth split



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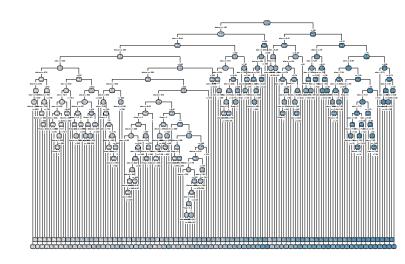
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Example regression tree – maximum possible splits



Regression trees

How are splits decided?

- 1 Take all possible *predictors* and all possible *cutpoints*
- 2 Split the data(sub)set at all combinations
- 3 Compute some **measure of discrimination** for all these i.e., a measure which determine which split is "best"
- 4 Select the predictor/split that most discriminates

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How are splits decided? – Continuous response

Select the predictor/split that most increases *between-class* variance (this decreases *pooled within-class* variance):

$$\sum_{\ell} \sum_{i} (y_{\ell,i} - \overline{y_{\ell}})^2$$

- $y_{\ell,i}$ value i of the target in leaf ℓ
- $\overline{y_l}$ is the mean value of the target in leaf ℓ

So the set of leaves are **more homogeneous**, on average, than the root.

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Example split (1)

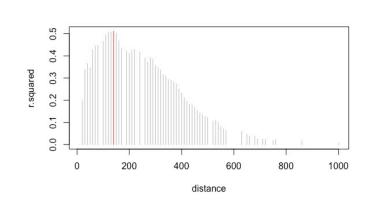
```
> # all the possible cutpoints for distance to river
> (distances <- sort(unique(meuse$dist.m)))</pre>
 [1]
       10
                       40
                                 60
                                                           120
            20
                  30
                            50
                                       70
                                                100
                                                     110
                                                                130
                                                                     140
                                                                          150
[15]
      160
           170
                190
                      200
                           210
                                220
                                      240
                                           260
                                                270
                                                     280
                                                           290
                                                                300
                                                                     310
                                                                           320
[29]
      330
           340
                350
                      360
                           370
                                380
                                      390
                                           400
                                                410
                                                     420
                                                           430
                                                                440
                                                                     450
                                                                          460
[43]
      470
           480
                490
                      500
                           520
                                530
                                      540
                                           550
                                                560
                                                     570
                                                           630
                                                                650
                                                                     660
                                                                          680
[57]
      690
           710
                720
                      750
                           760
                                860 1000
> for (i in 1:length(distances)) { # trv them all
  branch.less <- meuse$zinc[meuse$dist.m < distances[i]]
  branch.more <- meuse$zinc[meuse$dist.m >= distances[i]]
  rss.less <- sum((branch.less-mean(branch.less))^2)
  rss.more <- sum((branch.more-mean(branch.more))^2)
  rss <- sum(rss.less + rss.more)
  results.df[i,2:5] <- c(rss.less, rss.more, rss, 1-rss/tss)}
> # find the best split
> ix.r.squared.max <- which.max(results.df$r.squared)</pre>
> print(results.df[ix.r.squared.max,])
   distance rss.less rss.more
                                     rss r.squared
13
        140 7127795 3030296 10158091 0.510464
> # plot the results
plot(r.squared ~ distance, data=results.df, type="h",
     col=ifelse(distance==d.threshold."red"."grav"))
```

methods for predictive modelling DGR/罗大维

Data-driven

Example split (2): R^2 vs. cutpoint – distance to river

Try to split the **root node** on this predictor:



Best cutpoint is 140 m; this explains 51% of the total variance

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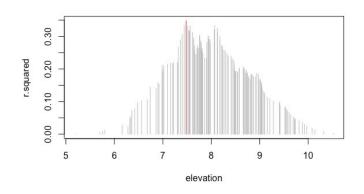
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Example split (3): R^2 vs. cutpoint – elevation

Try to split the **root node** on this predictor:



Best cutpoint is 7.48 m.a.s.l.; this only explains 35% of the total variance; so use the distance to river as the first split

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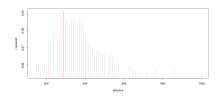
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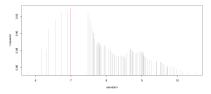
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Example split (4a): left first-level leaf

Try to split the **left first-level leaf** (101 observations):





Best cutpoint is 6.99 m.a.s.l.; this explains 93.0% of the variance *in this group*. Splitting at 290 m distance would explain 89.1%.

So split this leaf on *elevation* – it becomes an *interior node*

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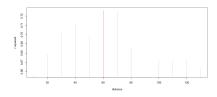
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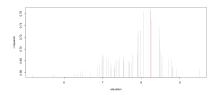
Spatial random forests

Data-driven v: model-driven methods

Example split (4b): right first-level leaf

Try to split the **right first-level leaf** (54 observations):





Best cutpoint is 8.23 m.a.s.l.; this explains 76.6% of the variance in this group. Splitting at 60 m distance would explain 72.6%.

So split on elevation – it becomes an interior node.

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Internal representation of the tree

```
node), split, n, deviance, yval
      * denotes terminal node
   1) root 155 1.513633e+01 2.556160
     2) dist.m>=145 101 4.652110e+00 2.388584
       4) elev>=6.943 93 2.835457e+00 2.349952
         8) dist.m>=230 78 1.735841e+00 2.311717
          16) elev>=9.028 29 3.657173e-01 2.218499
            32) dist.m>=670 8 7.842734e-03 2.107362 *
            33) dist.m< 670 21 2.214203e-01 2.260837
              66) elev>=9.5415 9 7.287443e-02 2.187184 *
              67) elev< 9.5415 12 6.310607e-02 2.316077 *
          17) elev< 9.028 49 9.689808e-01 2.366887
            34) dist.m>=250 47 9.067079e-01 2.359533
              68) dist.m>=525 10 1.400007e-01 2.302179
               136) dist.m< 660 8 5.166170e-02 2.262676 *
               137) dist.m>=660 2 2.591870e-02 2.460192 *
              69) dist.m< 525 37 7.249212e-01 2.375035
               138) dist.m< 510 36 6.193825e-01 2.366133
                 276) elev>=8.4485 13 1.107937e-01 2.319408 *
                 277) elev< 8.4485 23 4.641635e-01 2.392544
(etc.)
```

prediction

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Data-driven vs model-driven methods node) the node number, a binary representation of its position in the tree

• e.g., 67 = 1000011 right/left/left ...

split the splitting variable used at this node, the splitting value, and the splitting direction (\geq or <)

n number of observations at this node

deviance the sum of squared differences in fit of this mean value and the actual values for the observations in this node

yval the mean value of the observations in this node

The deviance for node i is computed as the total sum of squares:

$$D_i = \sum_i (y_j - \mu_i)^2$$

This is progressively smaller at lower levels of the tree.

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Controlling tree complexity

- Fitting a full tree, until there is only one observation per leaf, is always over-fitting to the sample set, and will not be a good predictor of the population.
- A full tree fits some **noise** as well as **structure**.
- Can control by the analyst or automatically by pruning (see below).
- Analyst can specify:
 - Minimum number of observations in a leaf (fewer: no split is attempted): minsplit
 - Maximum depth of tree: maxdepth
 - Minimum improvement in pooled within-class vs. between-class variance: cp (see below)

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Data-driven vs model-driven

Predicting with the fitted tree

- A simple 'model' is applied to each leaf:
 - Response variable continuous numeric: mean of observed data in leaf
 - Categorical variable: most frequent category in leaf
- Value at new location is predicted by running the covariate data down the tree

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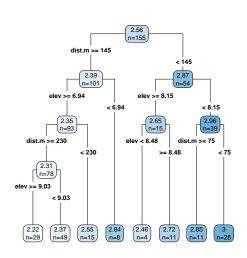
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Data-driven vs model-driven



Question: What is the predicted value for a point 100 m from the river and 9 m as I elevation?

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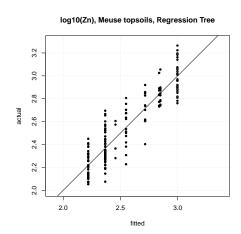
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Predictions at known points



Only one prediction per leaf, applies to all points falling in the leaf.

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Pruning – why?

- The splitting can continue until each calibration observation is in its own leaf
- This is almost always over-fitting to the current dataset
- What we want is a tree for the best **prediction**
- Solution: grow a full tree; then prune it back to a simpler tree with the best predictive power
 - \bullet Similar to using the ${\bf adjusted}\ R^2$ to avoid over-fitting a multiple linear regression

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The complexity parameter

The cp "complexity parameter": the increase in fit *below* which the tree is not further expanded

- Default value for the 'prune' function is 0.01 (1% increase in $R^2)$
- Can be set by the analyst during growing
 - rpart optional parameter
- Can also be used as a target for pruning
 - prune parameter

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- From the leaves backwards, remove splits that do not decrease the overall lack of fit by a factor of cp
- Q: How to decide on the value of cp that gives the best predictive tree?
- A: Use the cross-validation error, also called the out-of-bag error.
 - apply the model to the original data split K-fold (default 10), each time excluding some observations; compare predictions to actual values
 - Note how this fits the philosophy of data-driven approaches: predictive accuracy is the criterion

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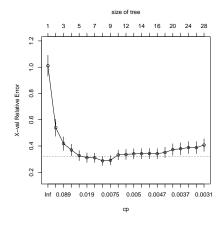
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X-validation error vs. complexity parameter



Horizontal line is 1 standard error above the minimum error. Usually choose the largest cp below this; here cp=0.01299 (about 1.3% improvement in R^2).

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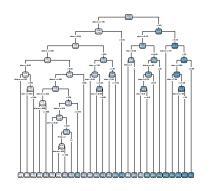
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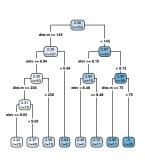
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Data-driven vs model-driven

Full and pruned trees





Full tree built with cp=0.003=0.3%; 27 leaves; pruned to 8 (cp=0.013=1.3%)

Interpretation: a noisy dataset if using these two predictors

methods

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Variable importance

- Unlike with linear regression we do not get any coefficient or its standard error for each predictor
- So to evaluate the importance of each predictor we see how much it's used in the tree
 - simple:
 - sum of gain in R^2 over all splits based on the predictor
 - complicated;
 - permute predictor values;
 - use these to re-build the tree;
 - compute cross-validation error;
 - the larger the difference, the more important
- This also includes surrogates, i.e., variables that could have substituted for missing values in another predictor.

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Regression trees

Variable importance – example

variableImportance 52.378203

elev 36.616987 soil 6.128099

dist.m

4.876711 ffreq

Normalized to sum to 100% of the gain in R^2

Distance to river is most important.

soil and ffreq were only important as surrogates for dist.m and/or elev, which were the only variables used in the pruned tree. prediction

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Surrogate variables

- What is to be done with observations missing a splitting variable?
 - e.g., in this case, a new point without a record of its flooding frequency
- Rather than classify the new observation as NA, maybe we can find surrogate variables in the training set: variables that can predict the value of the missing splitting variable at that split.
 - e.g., maybe *elev* is more useful than random assignment to predict flood frequency.
- These are ranked, and included in the **variable importance**, even if they are not used in the (pruned) tree.
- Observations missing the split variable are classified using the first surrogate; if that is missing also, the second surrogate, etc.
- Observations missing the split variable and all surrogates are randomly assigned to one of the branches.

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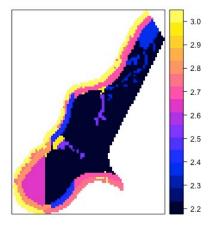
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Map predicted from Regression Tree



This tree: \log_{10} Zn predicted from dist (45% importance); E (17%); soil (15%); N (11%); ffreq. (11%).

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Sensitivity of Regression Trees

Sensitivity of Regression Trees to sample

- **Question**: how sensitive are Regression Trees to the sample?
- **Experiment**: build trees from random samples of 140 of the 155 observations (only 10% not used!)
 - How different are the optimized trees and the predictive maps?
 - What is the distribution of the optimal **complexity parameter** and the out-of-bag (predictive) error?

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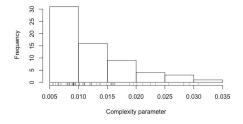
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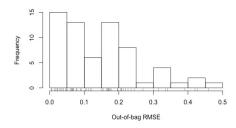
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Data-driven vs model-driven

Sensitivity: complexity and out-of-bag error





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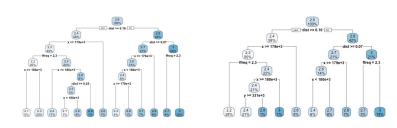
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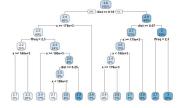
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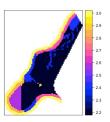
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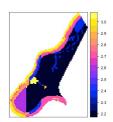
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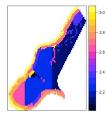
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Sensitivity: predictive maps







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Data-driven vs model-driven

Regression trees are sensitive to the observations

- This is a problem!
- **Solution**: why have one tree when you can have a **forest**?

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Data-driven vs model-driven

Classification trees

- Target variable is a categorical (classified) variable
- Tree structure is the same
- Stopping/pruning criterion is the minimum increase in node purity

(algorithmic) methods

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How are splits decided? – Categorical response

Select the predictor/split that minimizes the *impurity* of the set of leaves:

- Misclassification rate: $\frac{1}{N_m} \sum_{i \in R} I(y_i \neq k(m))$
 - N_m : number of observations at node m
 - R_m : the set of observations
 - k(m) is the majority class; I is the logical T/F function
- Impurity is maximal when all classes have same frequency, and minimal when only one class has any observations in the leaf

So the set of leaves are purer (less confusion), on average, than the root.

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Data-driven vs model-driven

Predicting with the fitted tree

- A simple 'model' is applied to each leaf:
 - Categorical variable: most frequent category in leaf (majority)
- Value at new location is predicted by running the covariate data down the tree

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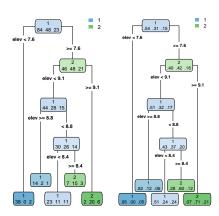
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Data-driven v model-driven

Classification tree – example

- (Meuse river) flood frequency class (3 levels) predicted from distance to river and elevation
- Result (pruned): number of observations in each class (left); proportion (right) – note class 3 not predicted!



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Random forests – motivation

- Instead of relying on a *single* (hopefully best) tree, maybe it is better to fit *many* trees.
- But...how to obtain multiple regression trees if we have only one data set?
 - Go into field and collect new sample data? too expensive and impractical.
 - Split the dataset and fit trees to the separate parts? Too few observations to build a reliable tree.
 - **Solution**: Use the *single* sample to generate an *ensemble* (group) of trees; use these together to predict.

Bagging and bootstrapping

Bagging (1)

- "Bag" = a group of samples "in the bag"; others "out-of-bag"
- Suppose we have a large sample that is a good representation of the study area
 - i.e., sample frequency distribution is close to population frequency distribution
- Generate a new sample is generated by sampling from the sample!

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Data-driven vs model-driven methods Standard method for sampling in bagging is called bootstrapping²

- Select same number of points as in sample
- Sample with replacement (otherwise you get the same sample)
- So some observations are used more than once!
- But, the sample is supposed to represent the population, so these could be values that would have been obtained in a new field sample.

²for historical reasons

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Data-driven v model-driven methods

Sampling with replacement

```
> # sample 20 times from (1, 2,... 20) with replacement
> (my.sample <- sample(1:20, 20, replace=TRUE))</pre>
    7 13 5 2 1 9 19 1
                                      9 12 4 11
> sort(my.sample)
 [1]
                                         9 11 11 12 13 19 20 20
> (1:20) %in% my.sample
                             in bag
 [1]
     TRUE
           TRUE FALSE
                       TRUE
                             TRUE
                                  TRUE
                                         TRUE FALSE
[10] FALSE
           TRUE
                 TRUE
                       TRUE FALSE FALSE FALSE FALSE
[19]
     TRUE
           TRUE
> !((1:20) %in% my.sample) # Out-of-bag
 [1] FALSE FALSE TRUE FALSE FALSE FALSE
                                               TRUE FALSE
[10]
     TRUE FALSE FALSE TRUE
                                   TRUE
                                         TRUE
                                               TRUE
                                                     TRUE
```

Example: 10 bootstrap samples from the integers 1 \dots 20 – sorted

Bagging and bootstrapping

```
b1 b2 b3 b4 b5 b6 b7
                          b8 b9 b10
                                    3
       3
                                    3
3
       3
           3
                        3
                               3
                                    5
              2
                     6
                            4
4
           6
                            5
                               3
                                   10
5
       5
           6
                           6
                               5
                                   10
6
    8
                   10
                               6
                                   11
   11
                   10
                                   13
8
   15
              8
                                   13
   15
         13
                   12
                                   13
             10
                       10
                   13
                                   14
  16
         15
                               8
             10 11 13 13
                                   14
      12 16 10 13 14 13 10
                                   14
      14 16 14 13 15 14 14 12
                                   15
            16 14 16 15 17 13
                                   16
             16 16
                   18 15
                                   16
         18
            17
                18 18 15 18
                                   16
         19 17 19 18 16 19 14
                                   17
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                19
                    19
            19 19
                   20 17
                                  20
      18
                              19
  19 18 20 19 19 20 19 20 20
                                  20
```

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Forests with bagging - method

- Fit a full regression tree to each bootstrap sample; do not prune
- Each bootstrap sample results in a tree and in a predicted value for any combination values of the predictors
- Prediction is the average of the individual predictions from the "forest" of regression trees
- Jumps in predictions are **smoothed**; more precise predictions

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Data-driven vs model-driven

Forest with bagging - limitations

- All predictors are tried at each split, so trees tend to be similar
- Some predictors may never enter into the trees → missing source of diversity
- Solution: random forest variation of bagging two sources of randomness
 - Random 1: sampling by bagging
 - Random 2: choice of predictors at each split (see next)

Data-driv (algorithmethods

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Random forests

- Multiple samples obtained by bootstrapping, used to build trees (as in bagging)
- Average predictions over all trees (as in bagging)
- Besides, in each internal node a random subset of splitting variables (predictors) is used
 - Extra source of diversity among trees
 - Predictors that are "outcompeted" in bagging by stronger competitors may now enter the group of trees

(algorithmic) methods

Classification & Regression Trees (CART)

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Data-driven v model-driven

R packages

randomForest older package, slow, some nice helper functions
ranger "a fast implementation of random forests or recursive
partitioning, particularly suited for high dimensional
data".

 Classification, regression, and survival forests are supported.

caret "Classification And REgression Training"; contains functions to streamline the model training process for complex regression and classification problems Modelling

Explanation v

(algorith

(CART)

Regression tree

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Data-driven vs model-driven methods

Selecting predictors at each split

- randomForest, ranger parameter mtry: Number of variables randomly sampled as candidates at each split.
 - ranger default $\lfloor \sqrt{p} \rfloor$, where p is number of possible predictors
 - example: 60 predictors $\rightarrow \lfloor \sqrt{60} \rfloor = \lfloor 7.74 \rfloor = 7$ tried at each split
 - randomForest default $\lfloor p/3 \rfloor$
 - example: 60 predictors $\rightarrow \lfloor 60/3 \rfloor = \lfloor 20 \rfloor = 20$ tried at each split
- Can be tuned with caret, see below.

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Other control parameters

- · number of trees in the forest
 - ranger parameter min.node.size
 - randomForest parameter ntree
 - default = 500
- · minimal node size
 - ranger parameter min.node.size
 - randomForest parameter nodesize
 - default = 5
- (optional) names of variables to always try at each split; weights for sampling of training observations (to compensate for unbalanced samples)

Explanation of prediction

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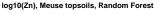
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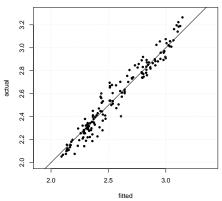
lodel tuning

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Data-driven vs model-driven methods

Fitted by RF vs. observed





Average prediction of many trees, comes close to actual value

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Out-of-bag ("OOB") evaluation

- In a bootstrap sample not all samples are present: sampling is with *replacement*.
- Sample data not in bootstrap sample: **out-of-bag** sample: these were *not* used to build the tree.
- These data can be used for evaluation ("validation"):
 - Use the tree fitted on the bootstrap sample to predict at out-of-bag data, i.e., observations not used in that bootstrap sample.
 - Compute **squared prediction error** for out-of-bag data.
- This gives a very good estimate of the true prediction error if the sample was representative of the population.

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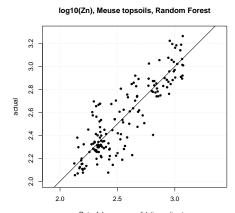
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Spatial random forests

Data-driven vs model-driven methods

Out-of-bag RF predictions vs. observed



Out-of-bag cross-validation estimates

Average prediction of many trees *not* using an observation. Further from actual value; **better estimate of predictive power**

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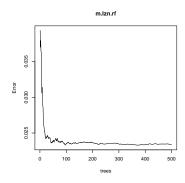
Model tuning

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Data-driven vs model-driven

How many trees are needed to make a forest?

- Plot mean squared out-of-bag error against number of trees
- Check whether this is stable
- If not, increase number of trees



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Variable importance

Importance quantified by permutation accuracy:

- randomize (permute) values of a predictor
 - so the predictor can not have any relation with the target
- build a random forest with this randomized predictors and the other (non-randomized) ones
- compute OOB error; compare with OOB error without randomization
 - the larger the difference, the more important
- Example:

```
% Increase in MSE under randomization ffreq 9.4 dist.m 67.5 elev 54.0
```

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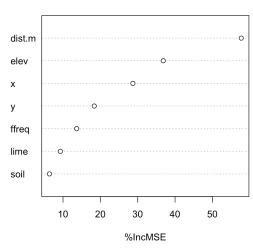
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Variable importance plot





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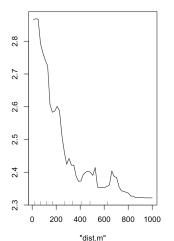
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Data-driven vs model-driven methods

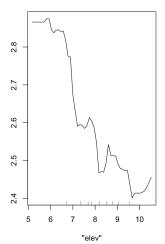
Partial dependence plots

The effect of each variable, with the others held **constant** at their means/most common class.

Partial Dependence on "dist.m"



Partial Dependence on "elev"



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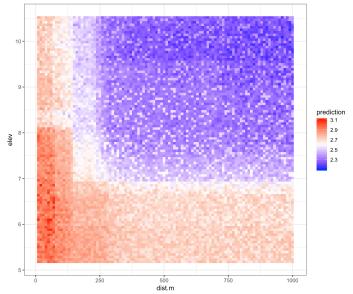
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Two-way partial dependence

Prediction of the forest for different values of dist.m and elev



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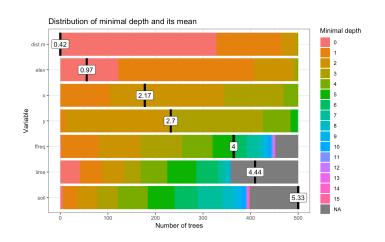
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Examining the forest – at what depth in the trees are predictors used?



Earlier in tree → most discriminating

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Variable importance for individual predictions

- It is also possible to see how much each variable influences each prediction separately
 - randomForest: option localImp=TRUE; ranger: option local.importance = TRUE
 - package iml "Interpretable Machine Learning"³
- Permutation tests, individual conditional expectation curves, Shapley values (see below)
- This shows which predictions are most influenced by which variables, *not* the importance of the variables overall

³https:

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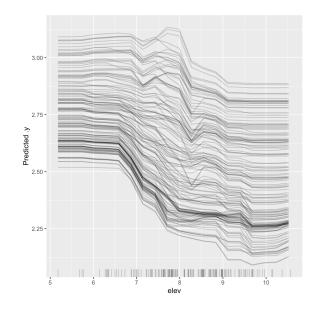
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Data-driven vs model-driven

Individual conditional expectation curves



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Shapley values

- An idea from game theory, developed by Shapley in 1953⁴
- This divides the contribution of the several variables to a prediction according to their average marginal contribution across all possible "coalitions" of variables
- "the only attribution method that satisfies the properties Efficiency, Symmetry, Dummy and Additivity, which together can be considered a definition of a fair payout."
- Shows the *direction* of the contribution, towards a higher or lower value
- Well-explained by Molnar⁵

⁴Shapley, L. S. (1953). A value for n-person games. In Contributions to the Theory of Games (AM-28), Volume II (pp. 307–318). Princeton University Press. https://doi.org/10.1515/9781400881970-018

⁵https://christophm.github.io/interpretable-ml-book/shapley.html

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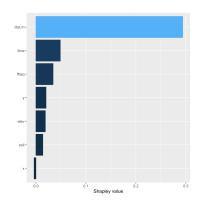
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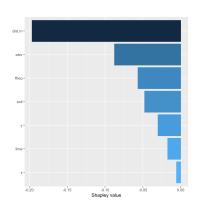
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Data-driven vs model-driven methods

Shapley values for the Meuse Zn 'ranger' model – by observation





(closest to river)

(furthest from river)

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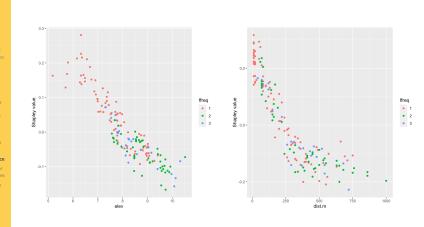
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Shapley values for the Meuse Zn 'ranger' model – by predictor



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Uncertainty of RF maps

- Recall: RF is built from many trees, each tree makes a prediction at each location
- These are averaged to get a "best" predictive map
- However, the set of predictions can be considered a probability distribution of the true value
- From this we can make a map of any **quantile**, e.g., 5% and 95% confidence limits, or prediction interval width

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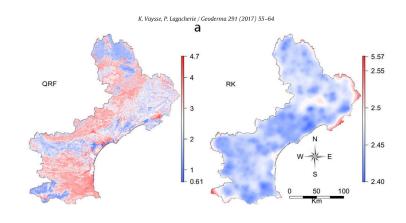
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Data-driven v model-driven methods

RF uncertainty vs. RK uncertainty



95% prediction interval for topsoil pH prediction from 2 024 point observations and 18 covariates Languedoc-Roussillon region (F)

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References for quantile random forests

- Meinshausen, N. (2006). Quantile regression forests. Journal of Machine Learning Research, 7, 983–999.
- Meinshausen, N., & Schiesser, L., 2015. Quantregforest: Quantile Regression Forests. R package. https://cran.r-project.org
- Vaysse, K., & Lagacherie, P. (2017). Using quantile regression forest to estimate uncertainty of digital soil mapping products. Geoderma, 291, 55-64. https://doi.org/10.1016/j.geoderma.2016.12.017

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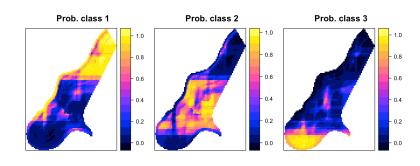
Random forests for categorical variables

- Target variable is **categorical**, i.e., a class
 - Example: Meuse river flooding frequency classes (every year, every 2–5 years, rare or none)
- Final prediction is the class predicted by the majority of the regression trees in the forest
- Can also see the probabilty for each class, by predicting with the model with the type="prob" argument to predict.randomForest.

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Random forests for categorical variables

Predicted class probabilty



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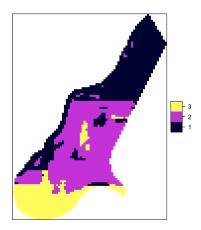
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Predicted most probable class



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Prediction uncertainty

- The vector of predicted probabilities can be used for several uncertainty measures
- These can be used to assess the certainty of the prediction, and maybe reject predictions that are too unsure.
- Confusion index: How much more probable is the majority class μ_{\max} to its next competitor $\mu_{(\max-1)}$

$$\mathrm{CI} = 1 - \{\mu_{\mathrm{max}} - \mu_{(\mathrm{max}-1)}\}$$

• **Shannon entropy**: Diversity of predictions. For a prediction *z* with *n* possible classes:

$$H_z = -\sum_{i=1}^n \hat{\pi}(z_i) \cdot log_n \hat{\pi}(z_i)$$

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Accuracy measures

- naïve agreement: how often a class in the training set is correctly predicted – see with a confusion matrix ("cross-classification")
- Out-of-bag (OOB) estimate of error rate
- Gini impurity: how often a randomly chosen training observation would be incorrectly assigned ...
 ...if it were randomly labeled according to the frequency

distribution of labels in the subset.

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Cross-classification matrix

A **confusion matrix** (a.k.a. cross-classification matrix) of actual (columns) vs. predicted (rows) classes:

Confusion matrix:

1 2 3 class.error

1 77 7 0 0.08333333

2 3 40 5 0.16666667

3 1 9 13 0.43478261

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Case weighting

- Recall: aim is predictive power
- Intuitively, the class proportions of OOB predictions should match those in the **population**
- If the sample proportions match the population proportions, this is a good basis
 - although notice, some classes may just be poorly-predicted by the predictor set
- If not, can use a priori class frequencies to weight the selection of observations for in/out-of-bag
 - ranger option case.weights
- Another use for case weights: some observations are more reliable than others (similar to weighted linear regression)

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Predictor selection

- Problem: large number of possible predictors, can lead to ...
 - Computational inefficiency
 - Difficult interpretation of variable importance, correlated predictors can substitute for each other
 - Meaningless good fits, even if using cross-validation⁶
- **Solution 1**: expert selection from "known" relations
 - this is then not pure "data mining" for unsuspected relations
- **Solution 2**: (semi-)automatic feature selection, see next.

⁶Wadoux, A. M. J.-C., *et al.* (2019). **A note on knowledge discovery and machine learning in digital soil mapping. European Journal of Soil Science**, 71, 133–136. https://doi.org/10.1111/ejss.12909

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Feature selection methods

Wrapper methods: "evaluate multiple models using procedures that add and/or remove predictors to find the optimal combination that maximizes model performance."

- risk of over-fitting
- high computational load

Filter methods: "evaluate the relevance of the predictors outside of the predictive models and subsequently model only the predictors that pass some criterion"

- does not account for correlation among predictors
- does not directly assess model performance

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Recursive feature elimination

- A "wrapper" method
- Implemented in caret::rfe "Backwards Feature Selection" function
- Algorithm: "Recursive Feature Elimination (RFE) incorporating resampling"
 - Partition data into training/test sets via resampling
 - 2 Start with full model, compute variable importance
 - for each proposed subset size
 - 1 Re-compute model with reduced variable sets
 - **2** Calculate performance profiles using test samples
 - 4 Determine optimum number of predictors

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Reference for feature selection

- From the documentation of the caret package (§5).
- Feature selection: https://topepo.github.io/caret/ feature-selection-overview.html
- Recursive feature elimination: https://topepo.github. io/caret/recursive-feature-elimination.html

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Data-driven v model-driven methods

- Similar to CART, but instead of single values at leaves it creates a multivariate linear regression for the cases in the leaf
- Advantage vs. CART: predictions are continuous, not discrete values equal to the number of leaves in the regression tree.
 - Also can be improved with nearest-neighbours, see below
- Advantage vs. RF: model coefficients at leaves can be interpreted
- Disadvantage: its algorithm is not easy to understand; however its results are generally quite good.

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Refinements to Cubist

- "Committees" of models: a sequence of models, where each corrects the errors in the previous one
- nearest-neighbours adjustment: modify model result at a prediction point from some number of neighbours in feature (predictor) space.

$$\widehat{\mathbf{y}}' = \frac{1}{K} \sum_{i=1}^{K} w_i \left[t_i + (\widehat{\mathbf{y}} - \widehat{t}_i) \right]$$
 (1)

where t_i is the actual value of the neighbour, \hat{t}_i is its value predicted by the model tree(s), and w_i is the weight given to this neighbour for the adjustment, based on its distance D_i from the target point. These are computed as $w_i = 1/(D_i + 0.5)$ and normalized to sum to one.

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Example cubist model

```
Rule 1/1: [66 cases, mean 2.288309, range 2.053078 to 2.89098, err 0.103603]
  if^^Ix > 179095, dist > 0.211846
  then outcome = 2.406759 - 0.32 \text{ dist}
Rule 1/2: [9 cases, mean 2.596965, range 2.330414 to 2.832509, err 0.116378]
  if^^Ix <= 179095, dist > 0.211846
  then outcome = -277.415278 + 0.000847 y + 0.56 dist
Rule 1/3: [80 cases, mean 2.772547, range 2.187521 to 3.264582, err 0.157513]
  if^^Idist <= 0.211846
  then outcome = 2.632508 - 2.1 \text{ dist} - 2.4e-05 \text{ x} + 1.4e-05 \text{ y}
Rule 2/1: [45 cases, mean 2.418724, range 2.10721 to 2.893762, err 0.182228]
  if^{r}Ix \le 179826, ffreq in {2, 3}
  then outcome = 128.701732 - 0.000705 x
Rule 2/2: [121 cases, mean 2.443053, range 2.053078 to 3.055378, err 0.181513]
  if^{Tdist} > 0.0703468
  then outcome = 30.512065 - 0.87 \text{ dist} - 0.000154 \text{ x}
Rule 2/3: [55 cases, mean 2.543648, range 2.075547 to 3.055378, err 0.125950]
  if^{-1}dist > 0.0703468, ffreq = 1
  then outcome = 37.730889 - 0.000314 \times -0.35 \text{ dist} + 6.5e-05 \text{ y}
Rule 2/4: [34 cases, mean 2.958686, range 2.574031 to 3.264582, err 0.139639]
  if^{Tdist} \le 0.0703468
```

then outcome = 2.982852 - 0.36 dist

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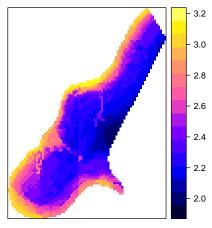
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Data-driven vs model-driven

Map predicted by Cubist

Optimized Cubist prediction



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Model tuning

- Data-driven models have parameters that control their behaviour and can significantly affect their predictive power.
 - CART: complexity parameter
 - randomForest: number of predictors to try at each split; minimum number of observations in a leaf; number of trees in the forest
 - too many predictors → trees too uniform, loss of diversity; too few → highly-variable trees, poor predictions
 - too few observations per leaf to imprecise prediction; too many
 → over-fitting
 - too few trees → sub-optimal model; too many trees → wasted computation
 - Cubist: number of committees; number of nearest neighbours
- The model can be **tuned** to **optimize** the selection of these.

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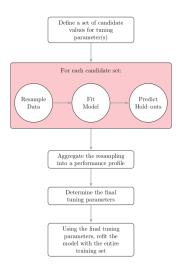
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Model tuning – flow chart



source: Kuhn, M., & Johnson, K. (2013). *Applied Predictive Modeling* (2013 edition). New York: Springer; figure 4.4

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Model tuning – algorithm

- For each combination of parameters to be optimized:
 - Split the dataset into some disjunct subsets, for example 10, by random sampling.
 - **2** For each subset:
 - 1 Fit the model with the selected parameters on all but one of the subsets (train subset).
 - Predict at the remaining subset, i.e., the one not used for model building, with the fitted model.
 - 3 Compute the goodness-of-fit statistics of fitting to the test subset
 - e.g., root mean square error (RMSE) of prediction; squared correlation coefficient between the actual and fitted values, i.e., R^2 against a 1:1 line.
 - **3** Average the statistics for the disjunct test subsets.
- **2** Search the table of results for the best results e.g., lowest RMSE, highest R^2 .

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Model tuning – R implementation

- caret "Classification And REgression Training" package
 - Kuhn, M. (2008). Building predictive models in R using the caret package. Journal of Statistical Software, 28(5), 1–26.
 - https://topepo.github.io/caret/index.html
 - can tune 200+ models; some built-in, some by calling the appropriate package
- method:
 - set up a vector or matrix with the parameter values to test, e.g, all combinations of 1 ...3 splitting variables to try, and 1 ...10 observations per leaf
 - 2 run the model for all of these and collect the cross-validation statistics
 - 3 select the best one and build a final model

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Model tuning example – random forest (1)

```
> ranger.tune <- train(x = preds, y = response, method="ranger",
              tuneGrid = expand.grid(.mtry = 1:3,
                                       .splitrule = "variance".
                                      .min.node.size = 1:10),
              trControl = trainControl(method = 'cv'))
> print(ranger.tune)
## Resampling: Cross-Validated (10 fold)
## Resampling results across tuning parameters:
##
##
           min.node.size
                           RMSE
                                     Rsquared
                                                 MAE
     mtrv
                                                 156.1662
##
                           199.7651
                                     0.8862826
     1
            1
##
                           200.5215
                                     0.8851154
                                                 156.3225
     1
                           200.6421
                                     0.8854146
                                                 156.2801
##
. . .
##
                           201.9809
                                     0.8793349
                                                 158.7097
     3
            8
##
     3
            9
                           202.9065
                                     0.8781754
                                                 159.7739
##
     3
           10
                           202.5687
                                     0.8788200
                                                 159.5980
## RMSE was used to select the optimal model
## Final values: mtry = 2, min.node.size = 6.
```

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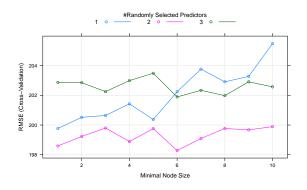
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Model tuning example – random forest (2)



Find the minimum RMSE; but favour simpler models (fewer predictors, larger nodes) if not too much difference

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Model tuning example – Cubist (1)

```
Summary of sample sizes: 139, 139, 140, 139, 139, 139, ...
## Resampling results across tuning parameters:
##
##
     committees
                 neighbors
                             RMSE
                                       Rsquared
                                                   MAE
                             0.1898596
                                        0.6678588
                                                   0.1405553
##
      1
##
                             0.1764705
                                        0.6953460
                                                   0.1189364
##
                             0.1654910
                                        0.7296723
                                                   0.1163660
##
      1
                             0.1623381
                                        0.7425831
                                                   0.1163285
##
                             0.1631900
                                        0.7453506
                                                   0.1192963
     12
                             0.1599994
                                        0.7533962
                                                   0.1139932
##
     12
                             0.1584434
                                        0.7617762
                                                    0.1153331
##
##
     12
                             0.1589143
                                        0.7622337
                                                   0.1165942
\##
```

RMSE was used to select the optimal model using the smallest value.

The final values: committees = 10, neighbors = 4.

Resampling: Cross-Validated (10 fold)

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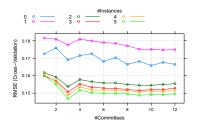
Spatial random forests

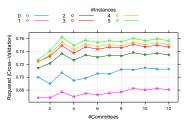
Data-driven vs model-driven

Model tuning example – Cubist (2)

Criterion: RMSE

Criterion: R²





Adding one neighbour reduces predictive power; adding 2 ...increases it; 3 is close to optimum

Committees improve predictive power; 3 is optimum

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Spatial random forests

- Random forests can use coördinates and distances to geographic features as predictors
 - e.g., E, N, distance to river, distance to a single point ...
- Can also use distances to multiple points as predictors
 - Distance buffers: distance to closest point with some range of values
 - Common approach: compute quantiles of the response variable and one buffer for each
 - Each sample point has a distance to the closest point in each quantile
- This uses separation between point-pairs of different values, but with no model.

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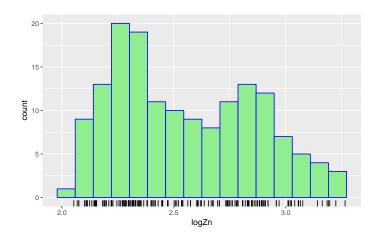
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$log_{10}Zn$ distribution – 16 quantiles



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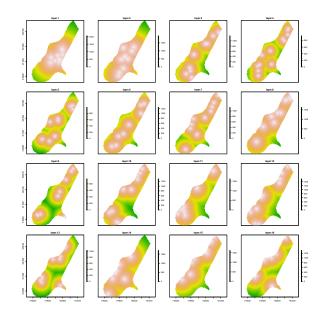
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Distance to closest point in each quantile



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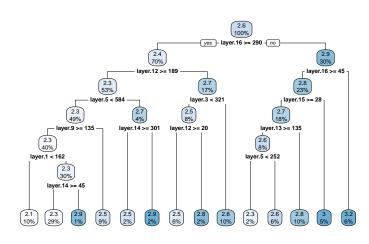
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Data-driven v model-driven

Regression tree on 16 distance buffers



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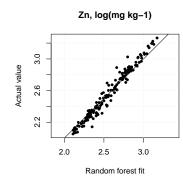
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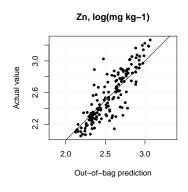
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Random forest prediction on 16 distance buffers





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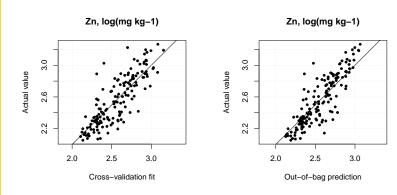
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Data-driven vs model-driven

OOB error vs. OK cross-validation error



OK RF

Note that RF does *not* use any *model* of spatial autocorrelation!

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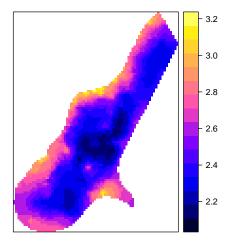
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Random forest map on 16 distance buffers



Resembles OK map, but no model was used.

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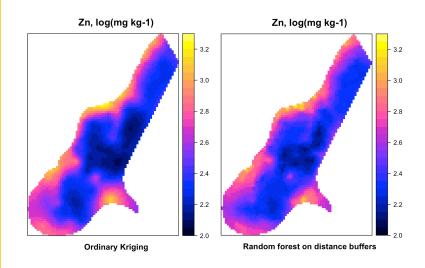
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Compare with Ordinary Kriging



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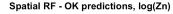
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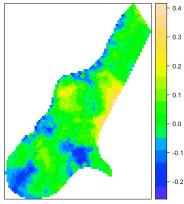
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Difference spatial RF - OK





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Reference for spatial random forests

 Hengl, T., Nussbaum, M., Wright, M. N., Heuvelink, G. B. M., & Gräler, B. (2018). Random forest as a generic framework for predictive modeling of spatial and spatio-temporal variables. PeerJ, 6, e5518. https://doi.org/10.7717/peerj.5518

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Conclusion: Data-driven vs. model-based methods

- Data-driven: main aim is predictive power
 - Individual trees can be interpreted (CART), but ensemble methods (random forests, Cubist ...) can not
 - can see variable importance overall and influence on each prediction
- Model-based: main aim is understanding processes
 - We hope the model is a simplified representation of the process that produced the observations
 - If the model is correct, predictions will be accurate

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Data-driven vs. model-driven methods

Conclusion: limitations

- Data-driven methods depend on their training observations
 - They have no way to extrapolate or even interpolate to unobserved areas in feature space
 - So the observations should cover the entire range of the population
- Model-based methods depend on a correct empirical-statistical model
 - Model is derived from training observations, but many models are possible
 - Various model-selection techniques
 - Wrong model → poor predictions, incorrect understanding of processes

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